

Model-based Boosting 2.0

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Abstract

We describe version 2.0 of the R add-on package *mboost*. The package implements boosting for optimizing general risk functions using component-wise (penalized) least squares estimates or regression trees as base-learners for fitting generalized linear, additive and interaction models to potentially high-dimensional data.

Keywords: component-wise functional gradient descent, splines, decision trees

1. Overview

The R add-on package *mboost* (Hothorn et al., 2010) implements tools for fitting and evaluating a variety of regression and classification models that have been suggested in machine learning and statistics. Optimization within the empirical risk minimization framework is performed via a component-wise functional gradient descent algorithm. The algorithm originates from the statistical view on boosting algorithms (Friedman et al., 2000; Bühlmann and Yu, 2003). The theory and its implementation in *mboost* allow for fitting complex prediction models, taking potentially many interactions of features into account, as well as for fitting additive and linear models. The model class the package deals with is best described by so-called structured additive regression (STAR) models, where some characteristic ξ of the conditional distribution of a response variable Y given features X is modeled through a regression function f of the features $\xi(Y|X = x) = f(x)$. In order to facilitate parsimonious and interpretable models, the regression function f is structured, that is, restricted to additive functions $f(x) = \sum_{j=1}^p f_j(x)$. Each model component $f_j(x)$ might take only

a subset of the features into account. Special cases are linear models $f(x) = x^\top \beta$, additive models $f(x) = \sum_{j=1}^p f_j(x^{(j)})$, where f_j is a function of the j th feature $x^{(j)}$ only (smooth functions or stumps, for example) or a more complex function where $f(x)$ is implicitly defined as the sum of multiple decision trees including higher-order interactions. The latter case corresponds to boosting with trees. Combinations of these structures are also possible. The most important advantage of such a decomposition of the regression function is that each component of a fitted model can be looked at and interpreted separately for gaining a better understanding of the model at hand.

The characteristic ξ of the distribution depends on the measurement scale of the response Y and the scientific question to be answered. For binary or numeric variables, some function of the expectation may be appropriate, but also quantiles or expectiles may be interesting. The definition of ξ is determined by defining a loss function ρ whose empirical risk is to be minimized under some algorithmic constraints (i.e., limited number of boosting iterations). The model is then fitted using

$$(\hat{f}_1, \dots, \hat{f}_p) = \operatorname{argmin}_{(f_1, \dots, f_p)} \sum_{i=1}^n w_i \rho \left(y_i, \sum_{j=1}^p f_j(x) \right).$$

Here $(y_i, x_i), i = 1, \dots, n$, are n training samples with responses y_i and potentially high-dimensional feature vectors x_i , and w_i are some weights. The component-wise boosting algorithm starts with some offset for f and iteratively fits residuals defined by the negative gradient of the loss function evaluated at the current fit by updating only the best model component in each iteration. The details have been described by Bühlmann and Yu (2003). Early stopping via resampling approaches or AIC leads to sparse models in the sense that only a subset of important model components f_j defines the final model. A more thorough introduction to boosting with applications in statistics based on version 1.0 of *mboost* is given by Bühlmann and Hothorn (2007).

As of version 2.0, the package allows for fitting models to binary, numeric, ordered and censored responses, that is, regression of the mean, robust regression, classification (logistic and exponential loss), ordinal regression,¹ quantile¹ and expectile¹ regression, censored regression (including Cox, Weibull¹, log-logistic¹ or lognormal¹ models) as well as Poisson and negative binomial regression¹ for count data can be performed. Because the structure of the regression function $f(x)$ can be chosen independently from the loss function ρ , interesting new models can be fitted (e.g., in geoaddivitive regression, Kneib et al., 2009).

2. Design and Implementation

The package incorporates an infrastructure for representing loss functions (so-called ‘families’), base-learners defining the structure of the regression function and thus the model components f_j , and a generic implementation of component-wise functional gradient descent. The main progress in version 2.0 is that only one implementation of the boosting algorithm is applied to all possible models (linear, additive, tree-based) and all families. Earlier versions were based on three implementations, one for linear models, one for additive models, and one for tree-based boosting. In comparison to the 1.0 series, the reduced code basis is easier to maintain, more robust and regression tests have been set-up in a more unified way. Specifically, the new code basis results in an enhanced and more user-friendly formula interface. In addition, convenience functions for hyperparameter selection, faster computation of predictions and improved visual model diagnostics are available.

1. Model family is new in version 2.0 or was added after the release of *mboost* 1.0.

Currently implemented base-learners include component-wise linear models (where only one variable is updated in each iteration of the algorithm), additive models with quadratic penalties (e.g., for fitting smooth functions via penalized splines, varying coefficients or bi- and trivariate tensor product splines, Schmid and Hothorn, 2008), and trees.

As a major improvement over the 1.0 series, computations on larger data sets (both with respect to the number of observations and the number of variables) are now facilitated by memory efficient implementations of the base-learners, mostly by applying sparse matrix techniques (package *Matrix*, Bates and Mächler, 2009) and parallelization for a cross-validation-based choice of the number of boosting iterations (per default via package *multicore*, Urbanek, 2009). A more elaborate description of *mboost* 2.0 features is available from the `mboost` vignette.²

3. User Interface by Example

We illustrate the main components of the user-interface by a small example on human body fat composition: Garcia et al. (2005) used a linear model for predicting body fat content by means of common anthropometric measurements that were obtained for $n = 71$ healthy German women. In addition, the women's body composition was measured by Dual Energy X-Ray Absorptiometry (DXA). The aim is to describe the DXA measurements as a function of the anthropometric features. Here, we extend the linear model by i) an intrinsic variable selection via early stopping, ii) additional terms allowing for smooth deviations from linearity where necessary (by means of penalized splines orthogonalized to the linear effect, Kneib et al., 2009), iii) a possible interaction between two variables with known impact on body fat composition (hip and waist circumference) and iv) using a robust median regression approach instead of L_2 risk. For the data (available as data frame `bodyfat`), the model structure is specified via a formula involving the base-learners corresponding to the different model components (linear terms: `bols()`; smooth terms: `bbs()`; interactions: `btree()`). The loss function (here, the check function for the 0.5 quantile) along with its negative gradient function are defined by the `QuantReg(0.5)` family (Fenske et al., 2009). The model structure (specified using the formula `fm`), the data and the family are then passed to function `mboost()` for model fitting.³

```
R> library("mboost")          ### attach package 'mboost'
R> print(fm)                  ### model structure

DEXfat ~ bols(age) + bols(waistcirc) + bols(hipcirc) + bols(elbowbreadth) +
  bols(kneebreadth) + bols(anthro3a) + bols(anthro3b) + bols(anthro3c) +
  bols(anthro4) + bbs(age, center = TRUE, df = 1) + bbs(waistcirc,
  center = TRUE, df = 1) + bbs(hipcirc, center = TRUE, df = 1) +
  bbs(elbowbreadth, center = TRUE, df = 1) + bbs(kneebreadth,
  center = TRUE, df = 1) + bbs(anthro3a, center = TRUE, df = 1) +
  bbs(anthro3b, center = TRUE, df = 1) + bbs(anthro3c, center = TRUE,
  df = 1) + bbs(anthro4, center = TRUE, df = 1) + btree(hipcirc,
  waistcirc, tree_controls = ctree_control(maxdepth = 2, mincriterion = 0))

R> ### fit model for conditional median of DEXfat
R> model <- mboost(fm,          ### model structure
```

2. Accessible via vignette("mboost", package = "mboost").

3. The complete R code for reproducing this example is given in the accompanying file `mboost-MLOSS.R`.

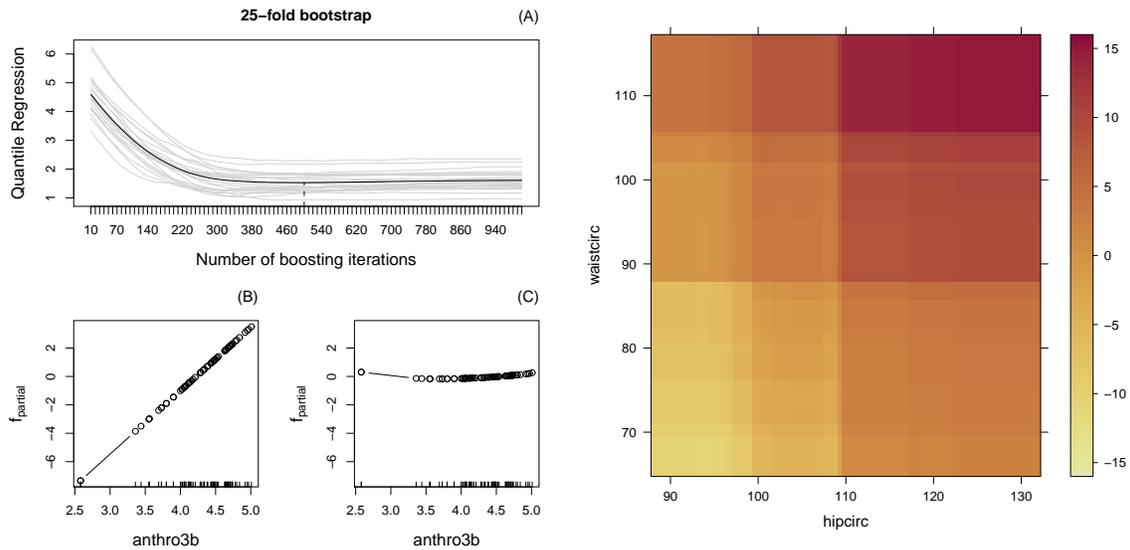


Figure 1: Out-of-bag empirical risk (A) indicating that 500 iterations are appropriate. Fitted model components for variable `anthro3b`, consisting of a linear (B) and smooth term (C). The right panel shows the interaction model component between `hip` and `waist` circumferences.

```
+           data = bodyfat,                ### 71 observations
+           family = QuantReg(tau = 0.5)) ### median regression
```

Once the model has been fitted it is important to assess the appropriate number of boosting iterations via the out-of-sample empirical risk. By default, 25 bootstrap samples from the training data are drawn and the out-of-bag empirical risk is computed (parallel computation if possible):

```
R> ### bootstrap for assessing the 'optimal' number
R> ### of boosting iterations
R> cvm <- cvrisk(model, grid = 1:100 * 10)
R> model[mstop(cvm)] ### restrict model to optimal mstop(cvm) iterations
```

Now, the final model is ready for a visual inspection:

```
R> plot(cvm)    ### depict out-of bag risk and
R> plot(model) ### selected components
```

The resulting plots are given in Figure 1. They indicate that a model based on three components, including a smooth function of `anthro3b` and a bivariate function of `hip` and `waist` circumference, provides the best characterization of the median body fat composition (given the model specification offered to the boosting algorithm). A hip circumference larger than 110 cm leads to increased body fat but only if the waist circumference is larger than 90 cm.

The sources of the `mboost` package are distributed at the Comprehensive R Archive Network under GPL-2, along with binaries for all major platforms as well as documentation and regression tests. Development versions are available from <http://R-forge.R-project.org>.

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